

Circles Questions for CDS, SSC & Railway Exams

Circle Quiz 1

Directions: Kindly study the following questions carefully and choose the right answer:

1. The diameter of a circle with centre at C is 50 cm. CP is a radial segment of the circle. AB is a chord perpendicular to CP and passes through P. CP produced intersects the circle at D. If DP = 18 cm, then what is the length of AB?

A. 24 cm B. 32 cm C. 40 cm D. 48 cm

2. A circle of radius 10 cm has an equilateral triangle inscribed in it. the length of the perpendicular drawn from the centre to any side of the triangle is

A. $2.5\sqrt{3}$ cm B. $5\sqrt{3}$ cm C. $10\sqrt{3}$ cm D. None of these

C. 3 : 2

3. In a $\triangle ABC$, AB = BC = CA. The ratio of the radius of the circumcircle to that of the incircle is

D. None of these

A. 2 : 1

4. Consider the following statements

 $B 3 \cdot 1$

I. The tangent of a circle is a line that meets the circle in one and only one point.

II. The tangent of a circle at the end point of the diameter is perpendicular to the diameter.

Which of the above statements is/are correct?

A. Only I B. Only II C. Both I and II D. Neither I nor II

5. A regular hexagon is inscribed in a circle of radius 5 cm. If x is the area inside the circle but outside the regular hexagon, then which one of the following is correct?

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A. 13 \text{ cm}^2 < x < 15 \text{ cm}^2B. 15 \text{ cm}^2 < x < 17 \text{ cm}^2C. 17 \text{ cm}^2 < x < 19 \text{ cm}^2D. 19 \text{ cm}^2 < x < 21 \text{ cm}^2
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6. AB and CD are two chords of a circle meeting externally at P. Then, which of the following is/are correct? I. $PA \times PD = PC \times PB$ II. $\triangle PAC$ and $\triangle PDB$ are similar. Select the correct answer using the codes given below. C. Both Land II D. Neither I nor II A. Only I B. Only II 7. Consider the following statements I. The perpendicular bisector of a chord of a circle does not pass through the centre of the circle. II. The angle in a semi-circle is a right angle. Which of the statements given above is/are correct? C. Both I and II D. Neither I nor II A. Only I B. Only II 8. Consider a circle with centre at O and radius r. Points A and B lie on its circumference and a point M lies outside of it such that M, A and O lie on the same straight line. Then, the ratio of MA to MB is A. equal to 1 B. equal to r C. greater than 1 D. less than 1 9. Consider the following statements in respect of two chords XY and ZT of a circle intersecting at P. I. $PX \cdot PY = PZ \cdot PT$ **II. PXZ and PTY are similar triangles.** Which of the statements given above is/are correct? C. Both I and II D. Neither I nor II A. Only I B. Only II **10.** ABC is an equilateral triangle inscribed in a circle D is any point on the arc BC. What is $\angle ADB$ equal to? B. 60° D. None of the above A. 90° C. 45°

Correct Answers:

1	2	3	4	5	6	7	8	9	10
D	D	А	С	А	D	В	D	С	В

18 cm

D

Explanations:

1.

In ∆ACP

CP = CD - PD = 25 - 18 = 7

Now, $AC^2 = CD^2 + AP^2$

: AP =
$$AC^2 - CD^2 = \sqrt{(25)^2 - (7)^2}$$

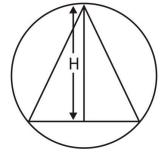
$$=\sqrt{625-49} = \sqrt{576} = 24$$
 cm

Similarly, PB = 24 cm



Hence, option D is correct.

Circumradius = $\frac{2}{3}$ × Height ∴ Height = $\frac{10 \times 3}{2}$ = 15 cm



So,

length of perpendicular drawn from center

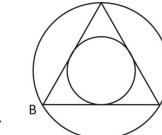
= 15 – 10 = 5 cm.

Hence, option D is correct.

3.

In ΔABC,

AB = BC = AC



Hence, $\triangle ABC$ is equilateral triangle.

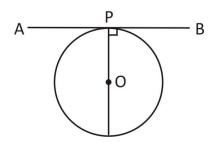
Let r be the radius of incircle and R be the radius of circumcircle.

Now, radius of incircle, $r = \frac{Side}{2\sqrt{3}} = \frac{AB}{2\sqrt{3}}$ and radius of circumcircle, $R = \frac{Side}{\sqrt{3}} = \frac{AB}{\sqrt{3}}$ So, the required ratio $= \frac{R}{r} = \frac{AB/\sqrt{3}}{AB/2\sqrt{3}} = \frac{2}{1}$ = 2 : 1. Hence, option A is correct.

By definition of tangent,

A tangent to a circle is straight line that touches the circle at a single point. Also, tangent at the end points of a diameter of a circle is perpendicular to the diameter.

So, both statements are correct.



Hence, option C is correct.

5.

OB = OA = radius

Also,
$$\angle AOB = 60^{\circ} \left(\frac{360^{\circ}}{6} = 60^{\circ}\right)^{\circ}$$

and $\angle OAB = \angle OBA = 60^{\circ}$ So, $\triangle AOB$ is an equilateral triangle. Then, E = 5 cm

So, Area, x = Area of circle – Area of hexagon

 $=\pi r^2 - \frac{3\sqrt{3}(a)^2}{2}$

 $=\frac{22}{7} \times (5)^2 - \frac{3\sqrt{3}(5)^2}{2} \qquad [\because r = a = 5]$

= 78.57 - 64.95 = 13.62 cm²

Hence, option A is correct.

6.

AB and CD are chords when produced meet externally at P.

$$\therefore \quad AP \times BP = CP \times DP$$

Now, as AC \nexists BD and \triangle PAC is not similar to \triangle PDB.

Hence, option D is correct.

7.

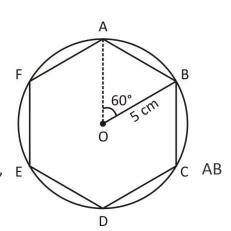
The perpendicular bisector of the chord of a circle always pass through the centre.

So, Statement I is wrong.

The angle in a semi-circle is a right angle.

So, Statement II is correct.

Hence, option B is correct.



В

D

8.

Since, secants ∠A and BN are intersecting at an exterior point M, then

 $LM \times AM = BM \times NM$ \Rightarrow MA = MN < 1 \cap M MBLM N B Hence, option D is correct. 9. When two chords of a circle are intersect internally, then they are divided in proportion. Ζ i.e. PX . PY = PZ . PT In ΔPXZ and ΔPTY , X 0 $\angle ZPX = \angle YPT$ (Vertically opposite angles) (angles in same segment) $\angle PZX = \angle PYT$ (angles in same segment) $\angle PXZ = \angle PTY$ ΔΡΧΖ ΔΡΤΥ Hence, the both statements are correct. Hence, option C is correct. 10. A $\angle ADB = \angle ACB = 60^{\circ}$ [: angles in the same segment are equal] Hencee, option B is correct. R D

