

## Mixed Maths Questions for SSC 10 + 2 and CGL Tier-I exams

## SSC Maths Quiz 4

Directions: Read the following questions carefully and choose the right answer.

1. If $x^{4}+\frac{1}{x^{4}}=322$, and $x>1$ then the value of $x^{3}-\frac{1}{x^{3}}$ is
A. 76
B. 54
C. 66
D. 36
2. Find the value of $\sin ^{2} 10+\sin ^{2} 20+\sin ^{2} 30+\ldots \ldots+\sin ^{2} 80$.
A. 2
B. 3
C. 1
D. 4
3. In the given figure, triangle $A B C$ is an isosceles triangle such that $A B=$ $B C$. Find $x, y$ and $z$ if angle CDE is $120^{\circ}$.
A. $x=60^{\circ}, y=60^{\circ}, z=60^{\circ}$
B. $x=30^{\circ}, y=40^{\circ}, z=60^{\circ}$
C. $x=40^{\circ}, y=60^{\circ}, z=60^{\circ}$
D. $x=50^{\circ}, y=40^{\circ}, z=60^{\circ}$
4. Find the value of $\frac{16}{\sqrt{3}}\left(\cos 50^{\circ} \cos 10^{\circ} \cos 110^{\circ} \cos 60^{\circ}\right)$

A. 1
B. 2
C. -1
D. -2
5. If the rate of income tax increases by $\mathbf{1 8 \%}$, net income decreases by $\mathbf{2 \%}$. What was the rate of income tax?
A. 10
B. 20
C. 15
D. 12
6. If $x+y+z=6 \sqrt{3}$ and $x^{2}+y^{2}+z^{2}=36$. Find $x: y$ : $z$.
A. $1: 1: 2$
B. $2: 3: 1$
C. $1: 1: 1$
D. $1: 2: 3$
7. The speed of boat is $10 \mathrm{~km} / \mathrm{hr}$ in still water and speed of current is $4 \mathrm{~km} / \mathrm{hr}$. A man covered 12 km upstream, took some rest and then covered 14 km downstream. Find the period of time for which he took rest if he took 4 hrs to cover his complete journey.
A. 0.5 hr
B. 1 hr
C. 1.5 hr
D. 1.25 hr
8. If $R$ and $r$ are respectively the circumradius and in radius of triangle having sides $40 \mathrm{~cm}, 41 \mathrm{~cm}$ and 9 cm , then find the value of $2(R+r)$.
A. 40
B. 49
C. 45
D. 44
9. In the given figure, the side $B C$ of $\triangle A B C$ is produced on both side, then $\angle 1+\angle 2$ is equal to
A. $\angle A+\angle 180^{\circ}$
B. $180^{\circ}-\angle \mathrm{A}$
C. $2 \angle A+180^{\circ}$
D. $\angle \mathrm{A}+90^{\circ}$
10. Find the value of $\cos ^{2} \theta\left(\sqrt{\frac{1+\sin \theta}{1-\sin \theta}}+\sqrt{\frac{1-\sin \theta}{1+\sin \theta}}\right)$
A. $\cos \theta$
B. $\frac{\cos \theta}{2}$
C. $2 \cos \theta$
D. $\sqrt{2} \cos \theta$


## Correct answers:

| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| A | D | A | C | A | C | B | B | A | C |

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## Explanation:

1. $\mathrm{x}^{4}+\frac{1}{\mathrm{x}^{4}}=322[\mathrm{x}>1]$ given

We know that, $\left[(a+b)^{2}=a^{2}+b^{2}+2 a b\right]$ Or, $\left[(a+b)^{2}-2 a b=a^{2}+b^{2}\right]$
So, $\left(x^{2}+\frac{1}{x^{2}}\right)^{2}-2 \times x^{2} \times \frac{1}{x^{2}}$
$=x^{4}+\frac{1}{x^{4}}$
Or, $\left(x^{2}+\frac{1}{x^{2}}\right)^{2}=322+2$
$\left(x^{2}+\frac{1}{x^{2}}\right)^{2}= \pm 18$
Also, $\left(x^{2}-\frac{1}{x^{2}}\right)^{2}+2 \times x \times \frac{1}{x}$
$=x^{2}+\frac{1}{x^{2}}$
$\left(x^{2}-\frac{1}{x^{2}}\right)^{2}+2=18$
$\left[\because(a-b)^{2}+2 a b=a^{2}+b^{2}\right]$
$\left(x-\frac{1}{x}\right)= \pm 4$

Now, Cubbing both sides, we get
$\mathrm{x}^{3}-\frac{1}{\mathrm{x}^{3}}-3 \times \mathrm{x} \times \frac{1}{\mathrm{x}}\left(\mathrm{x}-\frac{1}{\mathrm{x}}\right)=64$
Or, $x^{3}-\frac{1}{x^{3}}-3(4)=64$
$x^{3}-\underline{1}=12+64$

$$
x^{3}
$$

$\left(x^{3}-\frac{1}{x^{3}}\right)=76$

Hence, option A is correct.
2. We can rewrite above equation as
$\sin ^{2} 10+\sin ^{2} 80+\sin ^{2} 20+\sin ^{2} 70+\sin ^{2} 30+\sin ^{2} 60+\sin ^{2} 40+\sin ^{2} 50 \ldots .$. equation (A)

We know that $\sin ^{2} x+\sin ^{2}(90-x)=1$

Therefore equation A becomes
$1+1+1+1=4$
Hence, option D is correct.
3. Mehtod I:

Since quadrilateral CDEF is Cyclic quadrilateral, therefore
$\angle \mathrm{CDE}+\angle \mathrm{CFE}=180^{\circ}$
Therefore,
$\angle C F E=180^{\circ}-120^{\circ}=60^{\circ}$
We know that
Angles formed from two points on the same arc are equal .
Therefore
$x=\angle C A E=60^{\circ}$
Since $A B=B C$

Thus $x=\angle A C B=60^{\circ}$
By angle sum property of triangle $A B C$, we have
$x+x+\angle A B C=180^{\circ}$
$\angle A B C=180-2 x$
$\angle A B C=180-120=60^{\circ}$
$\angle A B C=y=60^{\circ}$ as vertically opposite angles are same.
Using angle sum property in $\triangle$ FBE ,we get
$60^{\circ}+60^{\circ}+z=180^{\circ}$

Thus $z=60^{\circ}$

## Method II:

In this question, CDEF will be a cyclic quadrilateral.
Therefore, the sum of the opposite angle i.e. angle $C D E=$ angle $C F E=180^{\circ}$
$120^{\circ}+\angle C F E=180^{\circ}$
$<C F E=180-120=60^{\circ}$
Now, if we take CE a chord then we know that the angle made by the same chord on any point of the circumference is equal therefore
$\angle C F E=\angle C A E=60^{\circ}=X-----$ (i)
Again, according to the question, $\mathrm{AB}=\mathrm{BC}$ therefore $\mathrm{x}=\angle \mathrm{ACB}=60^{\circ}$
In triangle $\mathrm{ABC},<\mathrm{X}+<\mathrm{ACB}+<\mathrm{ABC}=180^{\wedge} 0$
$60+60+<A B C=180$
$\angle A B C=180-120=60^{\circ}----$ (ii)
Now, AE and CF intersect each other at B

Therefore, $\angle \mathrm{ABC}=<\mathrm{FBE}=\mathrm{Y}=[60]^{\wedge} 0----$ (iii) (from the equation $\mathrm{I},<\mathrm{ABC}=60^{\circ}$ )
Now in the triangle FBE, $\angle F B E+\angle B E F+\angle B F E=60+60+Z=180$
By solving, $z=60^{\circ}$

Therefore, $x=y=z=60^{\circ}$

Hence, option A is correct answer.
4. We have $\operatorname{Cos} x \operatorname{Cos}(60-x) \operatorname{Cos}(60+x)=\operatorname{Cos} x(\operatorname{Cos} x \operatorname{Cos} 60+\operatorname{Sin} x$ $\left.\operatorname{Sin} 60^{\circ}\right)\left(\operatorname{Cos} x \operatorname{Cos} 60^{\circ}-\operatorname{Sin} x \operatorname{Sin} 60^{\circ}\right)$
$=\operatorname{Cos} x\left(\cos ^{2} x \operatorname{Cos}^{2} 60^{\circ}-\operatorname{Sin}^{2} x \operatorname{Sin}^{2} 60^{\circ}\right)$
$=\operatorname{Cos} x\left(\frac{1}{4} \cos ^{2}-\frac{3}{4} \sin ^{2} x\right)$
$=\frac{1}{4}\left(\operatorname{Cos}^{3} x-3 \operatorname{Cos} x\left(1-\operatorname{Cos}^{2} x\right)\right)$
$=\frac{1}{4}\left(4 \operatorname{Cos}^{3} x-3 \operatorname{Cos} x\right)$
$=\frac{1}{4} \operatorname{Cos} 3 x$

Thus,
$\cos x^{\circ} \cos (60-x)^{\circ} \cos (60+x)=\frac{1}{4} \cos (3 x)$
Therefore,
$\operatorname{Cos} 50^{\circ} \operatorname{Cos} 10^{\circ} \operatorname{Cos} 110^{\circ}=\frac{1}{4} \operatorname{Cos} 150^{\circ}$
$=\frac{1}{4}(-\sqrt{ } 3 / 2)=-\frac{\sqrt{ } 3}{8} \quad \ldots$ eq $A$
Also $\cos 60^{\circ}=\frac{1}{2} \quad$... eqB

Put values of eq.A and Eq.B in
$\frac{16}{\sqrt{3}}\left(\operatorname{Cos} 50^{\circ} \operatorname{Cos} 10 \operatorname{Cos} 110^{\circ} \operatorname{Cos} 60^{\circ}\right)$, we get
$=\frac{16}{\sqrt{3}} \times\left(-\frac{\sqrt{ } 3}{8}\right) \times \frac{1}{2}$
$=-1$
Option C is hence the correct answer.
5. $18 \%$ of income tax $=2 \%$ of net income
$\frac{\text { Income tax }}{\text { Net income }}=\frac{2}{18}=\frac{1}{9}$

Let the income tax be x and Net income be 9 x

Therefore total income $=x+9 x=10 x$

Rate of Income tax $=\frac{x}{10 x} \times 100 \%=10 \%$

Hence, option A is correct.
6. Sol We have $(a+b+c)^{2}=a^{2}+b^{2}+c^{2}+2 a b+2 b c+2 c a$

Therefore $(x+y+z)^{2}=(6 \sqrt{ } 3)^{2}$
$=x^{2}+y^{2}+z^{2}+2 x y+2 y z+2 z x=108$
$=36+2(x y+y x+z x)=108$
$=x y+y z+z x=36$......equation $A$
Comparing equation A with $\mathrm{x}^{2}+\mathrm{y}^{2}+\mathrm{z}^{2}=36$
We get $x^{2}=x y$ or $x=y$

Similarly we get $x=y=z$

Therefore $\mathrm{x}: \mathrm{y}: \mathrm{z}=1: 1: 1$
Thus option C is correct answer.
7. We know that

Downstream speed $=$ Speed of boat in still water + Speed of current

Upstream speed $=$ Speed of boat in still water - Speed of current.

Downstream speed $=10+4=14 \mathrm{~km} / \mathrm{hr}$

Upstream speed $=10-4=6 \mathrm{~km} / \mathrm{hr}$

Time taken to cover 12 km upstream $=12 / 6=2 \mathrm{hr}$

Time taken to cover 14 km downstream $=14 / 14=1$

Time for which he took rest $=4-3=1 \mathrm{hr}$

Hence, option B is correct.
8. We have,
$41^{2}=1681$
$40^{2}=1600$
$9^{2}=81$

Since, $41^{2}=40^{2}+9^{2}$

Therefore, Given triangle is a right angle triangle whose hypotenuse is 41 , and others two are perpendicular and base.

Sum of base and perpendicular $=49 \mathrm{~cm}$

We know In right angle triangle,
Inradius $=\frac{\mathrm{P}+\mathrm{B}-\mathrm{H}}{2}$
$=\frac{49-41}{2}=\frac{8}{2}=4 \mathrm{~cm}$

Also circumradius in right angle triangle $=$
$\frac{\mathrm{H}}{2}=\frac{41}{2} \mathrm{~cm}$
$R+r=4+\frac{41}{2}=\frac{49}{2}$
$2(R+r)=49 \mathrm{~cm}$

Hence option B is correct.
9. We know
$\angle A+\angle 5+\angle 6=180^{\circ}$
Also, $\angle 2=\angle A+\angle 6$
and $\angle 1=\angle A+\angle 5$

[Exterior angle is equal to sum of two opposite angels of triangle]
$\angle 1+\angle 2=2 \angle A+\angle 5+\angle 6$
$=\angle \mathrm{A}+180^{\circ}$

Hence, option A is correct.
10. $\cos ^{2} \theta\left(\sqrt{\frac{(1+\sin \theta)(1+\sin \theta)}{(1-\sin \theta)(1+\sin \theta)}}+\sqrt{\frac{(1-\sin \theta)(1-\sin \theta)}{(1+\sin \theta)(1-\sin \theta)}}\right)$

$$
\begin{aligned}
& \Rightarrow \cos ^{2} \theta\left(\sqrt{\frac{(1+\sin \theta)^{2}}{\left(1-\sin ^{2} \theta\right)}}+\sqrt{\frac{(1-\sin \theta)^{2}}{(1-\sin \theta)^{2}}}\right) \\
& \Rightarrow \cos ^{2} \theta\left(\sqrt{\frac{(1+\sin \theta)^{2}}{\cos ^{2} \theta}}+\sqrt{\frac{(1-\sin \theta)^{2}}{\cos ^{2} \theta}}\right) \\
& \Rightarrow \cos ^{2} \theta\left(\frac{1+\sin \theta}{\cos \theta}+\frac{1-\sin \theta}{\cos \theta}\right) \\
& \Rightarrow \cos ^{2} \theta\left(\frac{1+\sin \theta+1-\sin \theta}{\cos \theta}\right)=\frac{2 \cos ^{2} \theta}{\cos \theta}=2 \cos \theta
\end{aligned}
$$

Hence, option C is correct.

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